Problems: Non-LOS Propagation and Link Budget Analysis
EL-GY 6023. Wireless Communications

Prof. Sundeep Rangan

1. *Noise:* Suppose a receiver consists of an low noise amplifier with a gain of 30 dB and noise figure of 2 dB, followed by a second stage of amplification of another 20 dB with a noise figure of 10 dB.

   (a) What is the total noise figure and gain of the system?

   (b) Suppose a 10 dB attenuator is placed at the input of the LNA. What is the resulting overall gain and noise figure?

   (c) What if the attenuator is placed at the output of the LNA?

2. *SINR:* Suppose when a transmitter, TX1, sends data to a receiver RX without interference, the SNR is 10 dB. Now suppose that TX2 starts transmitting resulting in interference. Suppose TX2 transmits at the same power as TX1 and the path loss from TX2 to RX is 5 dB greater than the path loss from TX1 to RX. What is the resulting SINR from TX1 to RX when TX2 is transmitting?

3. *Reflection loss:* Let Γ be the reflection coefficient from an interface going from a characteristic impedance η_1 to η_2 and let Γ' be the reflection coefficient from η_2 to η_1. Show that if the angle of incidence is zero $\theta_i = 0$, $\Gamma = -\Gamma'$.

4. *SNR requirements:* A signal is received at power of P =-100 dBm and the noise power density (including the noise figure) is N_0 = -170 dBm/Hz. If a transmission of $b = 100$ bits requires an E_b/N_0 of 6 dB, what is the time to transmit the packet?

5. *Simulating a statistical model:* Write short MATLAB code to do the following. You do not need to run the code, just write the code.

   (a) Drop `nrx=1000` RX locations randomly in a circle of radius `radius = 100`m.

   (b) Assuming the transmitter is at the origin at a height `htx=2`m higher than the RX, compute the distances `dist` to the RXs.

   (c) Assuming a path loss model,

   $$PL = 32.4 + 14.3\log_{10}(d) + 20\log_{10}(f_c) + \xi, \quad \xi \sim \mathcal{N}(0, \sigma^2),$$

   generate random path losses to the RXs. Assume $\sigma = 4$ and $f_c = 2.3$ GHz.

   (d) Compute the SNR, E_s/N_0, to the RX. State all the parameters that you would need.

6. *Simulating a statistical model:* Consider an indoor propagation model where the path loss is,

$$PL = \text{FSPL}(d) + L_0 N, \quad N \sim \text{Poisson}(\alpha d),$$

where d is the distance between the TX and RX, FSPL(d) is the free-space path loss, N is the number of walls between a transmitter and receiver and N is modeled as a Poisson random variable where α is average number of walls per meter of distance. Write a MATLAB function

```
function pl = indoorPL(d, ... )
```

to generate random path loss values as function of a vector of distances. State all the other parameters this function needs. You may assume you have access to a function `fspl(lambda,d)` for the free-space path loss.

7. *Outage probability:* Suppose that a link has the following properties:

   - TX power, $P_{tx} = 20$ dBm
   - Bandwidth, $W = 20$ MHz
   - Noise power density (including noise figure) $N_0 = $ -170 dBm/Hz.

   Answer the following:

   (a) What is the maximum path loss, PL_{max}, that the link can have to meet an SNR target of 10 dB?

   (b) Suppose that the path loss is lognormally distributed with

$$PL = PL_0 + \xi, \quad \xi \sim \mathcal{N}(0, \sigma^2),$$

   where $PL_0 = 110$ dB and $\sigma = 8$ dB. What is the outage probability $P_{out} = \Pr(PL \geq PL_{max})$ using the value PL_{max} from part (a)? Your answer should have a Q-function. You can evaluate it with MATLAB's function `qfunc`.

   (c) A common model for indoor path loss is given by

$$PL = PL_0 + \xi + DN, \quad \xi \sim \mathcal{N}(0, \sigma^2),$$

   where N is the number of walls that the signal must pass through and D is the loss per wall. Suppose that we model the number of walls as a random variable with distribution:

$$P(N = n) = \begin{cases} 0.5 & \text{if } n = 0 \\ 0.3 & \text{if } n = 1 \\ 0.2 & \text{if } n = 2 \\ 0 & \text{else,} \end{cases}$$

   and the loss per wall is $D = 7$ dB. What is the outage probability P_{out}?