

# Propagation and Link-Budget Calculations. In-Class Exercises

These exercises accompany the lectures for this unit and should be done at the end of each section.

## Problem 1: Adding Noise and Measuring SNR

In this problem, we will simulate a simple cascade of two receiver elements:

- An LNA with gain  $GLna$  and noise figure  $NFLna$
- A mixer with unity gain and noise figure  $NFmix$

The received signal has power  $Prx$  and bandwidth  $B$ .

```
Prx = -80;      % RX power in dBm
NFLna = 6;     % Noise figure in the LNA in dB
GLna = 15;    % LNA gain in dB
NFmix = 13;   % mixer noise figure
B = 18e6;     % Bandwidth in Hz
```

Compute and print the effective noise figure.

```
% TODO
%   NFeff = ...
```

Assume the energy per sample in linear scale is  $E_s = Prx/B$ . Compute the SNR per sample,  $E_s N_0$ , including the effective noise figure.

```
% TODO
%   Es = ...
%   EsN0 = ...
```

We will now simulate this system. Generate  $nsym$  QPSK modulation symbols and scale them to the correct energy per symbol. Place the results in a vector  $s$ .

```
% Parameters
modRate = 4;      % num bits per symbol (4=16 QAM)
M = 2^modRate;   % QAM order
nsym = 10000;    % num symbols

% TODO
%   sym = ...
```

Now simulate the receiver:

- Add the thermal noise of the LNA
- Scale the signal by the LNA gain
- Add the thermal noise of the mixer

For the thermal noise in the LNA and mixer use the `comm.ThermalNoise` class. Store the results in a vector `r`. Plot the received constellation.

```
% TODO:
%   r = ...
```

Compute the SNR

$$EsNoMeas = 10 \cdot \log_{10} \left( \frac{E|G*s|^2}{E|r - G*s|^2} \right)$$

where  $G$  is the receiver gain in linear scale and  $E(\cdot)$  denotes the average value. Measure and print `EsNoMeas` and compare with the expected value.

```
% TODO
%   EsNoMeas = ...
```

In many cases, we do not know the gain  $G$ , so it has to be estimated to compute the SNR. Suppose that we have a model:

$$r = G*s + d, \quad d = \text{CN}(0, N0)$$

where  $G$  is the unknown gain, and  $N0$  is the unknown noise variance. We can estimate the gain and noise variance via linear regression:

$$\begin{aligned} \hat{G} &= (r'*s)/(s'*s); \\ \hat{N0} &= (1/n)*\|r - \hat{G}*s\|^2 = (1/n)*(r'*r - (r'*s)^2/(s'*s)) \\ \hat{Eshat} &= (1/n)*|\hat{G}|^2*\|s\|^2 \end{aligned}$$

This gives and SNR estimate:

$$\begin{aligned} EsN0hat &= \hat{Eshat} / \hat{N0hat} \\ &= |\hat{G}|^2*(s'*s) / (r'*r - |r'*s|^2/(s'*s)) \\ &= |r'*s|^2 / (s'*s) / (r'*r - |r'*s|^2/(s'*s)) \\ &= |r'*s|^2 / ((r'*r)*(s'*s) - |r'*s|^2) \\ &= \rho / (1 - \rho) \end{aligned}$$

where  $\rho$  is the correlation coefficient:

$$\rho = |r'*s|^2/(r'*r)*(s'*s)$$

Use this estimate to estimate the SNR.

```
% TODO
%   EsN0hat = ...
```

## Problem 2. Estimating the SNR Requirements for LTE

In this problem, we will see how the performance of a commercial LTE system compare to the Shannon theory. The LTE standard 36.942 provides a number of details of how to evaluate the performance of the system in various scenarios. You can find any of the 3GPP standards by googling, e.g. "3GPP 36.942". Below is a table from that document that shows the code performance as a function of the SNR for the uplink and downlink.

**Table A.2 Look-Up-Table of UL and DL Throughput vs. SNIR for Baseline E-UTRA Coexistence Studies**

Throughput					Throughput				
SNIR	bps/Hz		kbps per 375kHz RB		SNIR	bps/Hz		kbps per 375kHz RB	
dB	DL	UL	DL	UL	dB	DL	UL	DL	UL
-15	0	0	0	0	6	1.39	0.93	521	347
-14	0	0	0	0	7	1.55	1.04	582	388
-13	0	0	0	0	8	1.72	1.15	646	430
-12	0	0	0	0	9	1.90	1.26	711	474
-11	0	0	0	0	10	2.08	1.38	778	519
-10	0.08	0.06	31	21	11	2.26	1.51	847	565
-9	0.10	0.07	38	26	12	2.44	1.63	917	611
-8	0.13	0.08	48	32	13	2.63	1.76	988	658
-7	0.16	0.10	59	39	14	2.82	1.88	1059	706
-6	0.19	0.13	73	48	15	3.02	2.00	1131	750
-5	0.24	0.16	89	59	16	3.21	2.00	1204	750
-4	0.29	0.19	109	73	17	3.41	2.00	1277	750
-3	0.35	0.23	132	88	18	3.60	2.00	1350	750
-2	0.42	0.28	159	106	19	3.80	2.00	1424	750
-1	0.51	0.34	190	127	20	3.99	2.00	1498	750
0	0.60	0.40	225	150	21	4.19	2.00	1572	750
1	0.71	0.47	265	176	22	4.39	2.00	1646	750
2	0.82	0.55	308	206	23	4.40	2.00	1650	750
3	0.95	0.63	356	237	24	4.40	2.00	1650	750
4	1.09	0.72	408	272	25	4.40	2.00	1650	750
5	1.23	0.82	463	309					

In the github folder, you will find an Excel file with this data. You can read it via the command which will load the data into a table T .

```
T = readtable('lte_mcs.xlsx');
```

Now, read the SNR and downlink spectral efficiency from the table into vectors snr and se\_dl. You can use the table2array function. Plot the se\_dl vs. snr .

```
% TODO
% snr = ...
% se_dl = ...
```

On the same plot as above, plot the Shannon rate vs. SNR. You should see that the LTE value is lower.

```
% TODO:
% se_shannon = ...
```

Fit a model for the LTE DL rate:

$$se\_dl\_hat = \alpha * \log_2(1 + 10^{(0.1 * snr)})$$

where alpha is a parameter that we will fit. Fit this model using the data for SNR from -10 to 21 dB. To fit a model of the form  $y_i = \alpha * x_i$ , you can use the regression formula:

```
alpha = \sum_i (x_i*y_i) / \sum_i x_i^2
```

Print alpha. Also add the line `se_dl_hat` vs. `snr` to the previous plot.

```
% TODO:  
% alpha = ...  
% se_dl_hat = ...
```

### Problem 3: Simulating Path Loss Variations

Suppose the TX power is  $P_{tx}$  and the path loss can be modeled as a random variable as follows:

- The channel is either LOS or NLOS with probability  $\text{ProbLos}$  and  $1-\text{ProbLos}$ , respectively.
- If the channel is LOS, the path loss is lognormally distributed with mean  $\text{PLLos}$  and standard deviation  $\text{stdLos}$ .
- If the channel is NLOS, the path loss is lognormally distributed with mean  $\text{PLNlos}$  and standard deviation  $\text{stdNlos}$ .

Generate  $n=10000$  channel instances and plot the histogram of the received power. You may use the MATLAB histogram function.

```
Ptx = 15;           % Tx power in dBm  
ProbLos = 0.4;     % LOS probability  
PLNlos = 80;       % Path loss for LOS (dB)  
PLLos = 100;       % Path loss for NLOS (dB)  
stdLos = 8;        % Path loss std dev for LOS (dB)  
stdNlos = 4;       % Path loss std dev for LOS (dB)  
n = 10000;         % number of samples  
  
% TODO  
% Prx = ...  
% histogram(Prx, ...);
```